A Correction of the Paper "Non-Characteristic Cauchy Problems and Generalized Goursat Problems in R""

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I want to thank Karl Erik Sandvold, Oslo. He has pointed out to me that the boundary conditions in Theorem 3 [1] must be changed. Otherwise the theorem is false. We change them in the following way. Let the functions φ_i satisfy the conditions in the remark after Theorem 3. Substitute in (4.4) v by $D^{\beta}u$. Then we get a somewhat more general (4.8). Define

$$\gamma_i^{i'} = \beta_i$$
, $1 \leq j < j'$, $\gamma_i^{i'} = 0$, $j' \leq j \leq n$.

Then (4.9) is written as

$$(4.9) D^{\gamma}D^{\gamma i}u(x) = 0, \varphi_i(x) = 0, \gamma \leq \beta - \gamma^i,$$

$$\gamma_i < \beta_i, 1 \leq i \leq n, x \in A.$$

If we know $D^{\beta}u$ and if (4.9) is true then (4.8) is true for every $\alpha \leq \beta$, Conversely, if (4.8) is true then (4.9) is satisfied. The boundary conditions in Theorem 3 should then be given by the new (4.9). Looking at the example by Chu and Diaz mentioned in the introduction of [1] this corresponds to giving the value of u(x, y, z) on x = 0, and y = 0, and the value of $u_{xy}(x, y, z)$ on the third surface. It should be pointed out that also the noncharacteristic Cauchy problem can be written as a generalized Goursat problem. But then the boundary values remain unchanged. This is also true for the Goursat problem if $\varphi_i = x_i$, $1 \leq j \leq n$. See [2].

REFERENCES

 J. Persson, Non-characteristic Cauchy problems and generalized Goursat problems in Rⁿ, J. Math. Mech., 18 (1969) 1087-1094.

[2] ———, Theorems for continuous solutions of generalized Goursat problems, Mathematiche, 24 (1969) 108-136.

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