Free Boundary Problems for Parabolic Equations II. Evaporation or Condensation of a Liquid Drop

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Introduction. We shall refer to [2] as Part I. In Part I we proved the existence and uniqueness of the solution of Stefan problems for all future time. In this Part II we shall discuss problems of condensation and evaporation of one liquid drop surrounded by vapor of its own substance. We proceed to describe the main results.

If the initial vapor density on the surface of the drop is equal to the saturation density, then in case of condensation ($\alpha < 0$) existence and uniqueness are asserted for all future times and in case of evaporation ($\alpha > 0$) as long as the radius s(t) of the drop remains positive. Here α is a certain physical quantity which in case $\alpha < 0$ is assumed to be sufficiently small, and in case $\alpha > 0$ is assumed to be < 1. If the initial vapor density on the surface of the drop is not

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